

1) a) $P(2) = 61$

$P'(2) = A(2) - L(2)$

$= -0.401 \rightarrow M$

$P(2.5) \approx 6 + M(2.5 - 2)$

$= 6.201$

b) $P''(5) = A'(5) - L'(5)$

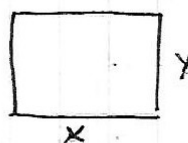
$= -0.679$

The rate of change of the number of people in the venue is decreasing at a rate of 0.679 hundreds of people per hour per hour.

c) If $P'(t)$ changes from neg to positive, then $A(t) - L(t)$ changes from neg. to pos.

This occurs at $t = 6.548$

d)



$x = 16 \quad \frac{dx}{dt} = 6$

$y = 10 \quad \frac{dy}{dt} = -3$

$$A = xy \quad \frac{dA}{dt} = x \frac{dy}{dt} + y \frac{dx}{dt}$$

$$= -48 + 60$$

$$= 12 \text{ ft}^2/\text{sec}$$

2) a) $w'(t) = \frac{1}{3}(t-4)$

$w'(7) = 1 \text{ ft}/\text{hour}$

At $t = 7$, the depth of water in the zoo aquarium is increasing at a rate of 1 ft/hour

b) $w(2) = \frac{32}{5}$

$w'(t) = -\frac{\pi}{10} \sin\left(\frac{\pi t}{4}\right)$

$w'(2) = -\frac{\pi}{10}$

$L(t) = \frac{32}{5} - \frac{\pi}{10}(t-2)$

$w(2.5) \approx \frac{32}{5} - \frac{\pi}{20} \geq 6$

c) $\lim_{t \rightarrow 2} \frac{w(t) - t^2 - \frac{12}{5}}{t-2} \rightarrow \frac{\frac{32}{5} - 4 - \frac{12}{5}}{0} \rightarrow \frac{0}{0}$

$$\frac{L'H}{\lim_{t \rightarrow 2} \frac{w'(t) - 2t}{1}} = w'(2) - 2t$$

$$= \left[-\frac{\pi}{10} - 4 \right]$$

$$3) a) x_p(t) = \frac{e^{2-t} - 2t}{e^{2-t} + 3t}$$

$$v_p(t) = \frac{(e^{2-t} + 3t)(-e^{2-t} - 2) - (e^{2-t} - 2t)(-e^{2-t} + 3)}{(e^{2-t} + 3t)^2}$$

$$= \frac{-e^{4-2t} - 2e^{2-t} - 3te^{2-t} - 6t + e^{4-2t} - 3e^{2-t} - 2te^{2-t} + 6t}{(e^{2-t} + 3t)^2}$$

$$= \frac{-5e^{2-t} - 5te^{2-t}}{(e^{2-t} + 3t)^2}$$

$$b) x_Q(2) = 5 \quad x_P(2) = -\frac{2}{3} < x_Q(2)$$

$$v_P(2) = \frac{-5 - 10}{36} = -\frac{15}{36} < 0 \quad \text{moving left}$$

Particle P is moving away from Particle Q.

$$c) v_Q(t) = 3t^2 - 6t$$

$$a_Q(t) = 6t - 6$$

$$a_Q(2) = 6$$

$$d) \lim_{t \rightarrow \infty} x_P(t) = -\frac{2}{3} \quad \lim_{t \rightarrow \infty} x_Q(t) = \infty$$

Particle P will approach position $x = -\frac{2}{3}$

Particle Q's position is unbounded